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**Probabilistic Scheduling**

Inventor(s):  
Caroline E. Matheson  
Marc Shapiro

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## **PROBABILISTIC SCHEDULING**

## **TECHNICAL FIELD**

The described subject matter relates to scheduling tasks. More particularly, the subject matter relates to scheduling based on probabilities associated with tasks.

## **BACKGROUND**

Scheduling programs facilitate scheduling of tasks that require resources within given time periods. Typically, the scheduling program receives requests for resources needed for the tasks. The scheduling program then attempts to allocate limited resources to tasks that compete for those resources. Based on the allocation, the scheduling program schedules the tasks. For example, a scheduling program may have five conference rooms to assign among five meetings. The meetings may have constraints, such as number of attendees, minimum time duration, etc. Based on the constraints, the scheduling program chooses time slots and resources for the tasks.

Unfortunately, typical task scheduling problems are not as simple as allocating five conference rooms among five meetings. In a hospital setting, for example, there may be many types of medical rooms, staff, equipment, and the like, which can be allocated among hundreds of patients or medical operations, which may require resources in the alternative or in combinations. For example, a medical operation may require either resource “a” or “b” but not both, while

1 another operation may require both resources “c” and “d.” As the size and  
2 complexity of task scheduling problems increase, optimal solutions are more  
3 difficult to achieve, particularly in an efficient manner.

4 One task scheduling technique traditionally used is a “brute force”  
5 technique. The brute force technique involves representing all possible tasks and  
6 their resource requirement alternatives and combinations in a tree structure, and  
7 then analyzing every path in the tree to determine which path gives best results.  
8 For simple task scheduling problems, the brute force method may work  
9 satisfactorily; however, when the problem becomes complex, the tree structure  
10 becomes correspondingly complex, with countless alternative paths to be analyzed.  
11 The analysis of every path in such a complex tree structure can become NP  
12 (nondeterministic polynomial time) hard; i.e., computationally impractical. As a  
13 result, solving a complex task scheduling problem using brute force methods can  
14 be extremely inefficient and/or unworkable.

17 Other task scheduling algorithms apply heuristics that are not well founded.  
18 These algorithms often employ task scheduling rules that are not based on  
19 scientific or logical reasoning, but rather intuitive notions. One heuristic technique  
20 employs “greedy” heuristics in which the solution is constructed sequentially  
21 without regard for the effect that a resource allocation choice might have upon  
22 other requested tasks. Greedy algorithms are attractive due to their simplicity.  
23 While a greedy technique may yield optimal results sometimes, it can yield  
24

1 extremely sub-optimal results. As with other heuristic techniques, the success, or  
2 lack of success, of a greedy technique is typically haphazard.

3

4 **SUMMARY**

5 Implementations described and claimed herein solve the discussed  
6 problems, and other problems, by providing task scheduling methods and systems.  
7 Exemplary implementations may apply probabilities of influence to resource  
8 allocation, and may schedule tasks based on whether, and to what degree, the  
9 resource allocation influences a task.

10

11 A method includes generating a cost associated with each of a plurality of  
12 tasks to be scheduled, and scheduling the minimum cost task if the minimum cost  
13 task successfully executes. Generating may include determining a pair-wise  
14 probability representing a probability that two tasks in the plurality of tasks  
15 conflict with each other.

16

17 A system includes a cost generator generating costs associated with a  
18 plurality of tasks, the costs based on probabilities that a task influences another  
19 task, and a scheduling engine operable to schedule the task with the least cost.

20

21

22 **BRIEF DESCRIPTION OF THE DRAWINGS**

23 Fig. 1 illustrates an exemplary scheduling engine implementing operations  
24 for probabilistic scheduling of tasks.

1 Fig. 2 is a hierarchical arrangement of a main task log, tasks, resource  
2 containers, and named resources.

3 Fig. 3 is a scheduling operation flow having exemplary operations for  
4 probabilistically scheduling tasks.

5 Fig. 4 is a cost tabulating operation flow having exemplary operations for  
6 generating costs associated with tasks.

7 Fig. 5 illustrates a user interface that may be employed by a scheduling  
8 engine to receive scheduling input and present scheduling output.

10 Fig. 6 illustrates another user interface that may be employed by a  
11 scheduling engine to receive scheduling input including constraints.

12 Fig. 7 illustrates an exemplary system that provides a suitable operating  
13 environment to schedule tasks in accordance with the systems, methods, and user  
14 interfaces described in Figs. 1-6.

16

17 **DETAILED DESCRIPTION**

18 Turning to the drawings, various methods are illustrated as being  
19 implemented in a suitable computing environment. Various exemplary methods  
20 are described in the general context of computer-executable instructions, such as  
21 program modules, being executed by a personal computer and/or other computing  
22 device. Generally, program modules include routines, programs, objects,  
23 components, data structures, etc. that perform particular tasks or implement  
24

1 particular abstract data types. Moreover, those skilled in the art will appreciate  
2 that various exemplary methods may be practiced with other computer system  
3 configurations, including hand-held devices, multi-processor systems,  
4 microprocessor based or programmable consumer electronics, network PCs,  
5 minicomputers, mainframe computers, and the like. Various exemplary methods  
6 may also be practiced in distributed computing environments where tasks are  
7 performed by remote processing devices that are linked through a communications  
8 network. In a distributed computing environment, program modules may be  
9 located in both local and remote memory storage devices.

10  
11 In some diagrams herein, various algorithmic acts are summarized in  
12 individual “blocks”. Such blocks describe specific actions or decisions that are  
13 made or carried out as a process proceeds. Where a microcontroller (or  
14 equivalent) is employed, the flow charts presented herein provide a basis for a  
15 “control program” or software/firmware that may be used by such a  
16 microcontroller (or equivalent) to effectuate the desired control. As such, the  
17 processes are implemented as machine-readable instructions storable in memory  
18 that, when executed by a processor, perform the various acts illustrated as blocks.

19  
20 Those skilled in the art may readily write such a control program based on  
21 the flow charts and other descriptions presented herein. It is to be understood and  
22 appreciated that the subject matter described herein includes not only devices  
23 and/or systems when programmed to perform the acts described below, but the  
24  
25

1 software that is configured to program the microcontrollers and, additionally, any  
2 and all computer-readable media on which such software might be embodied.  
3 Examples of such computer-readable media include, without limitation, floppy  
4 disks, hard disks, CDs, RAM, ROM, flash memory and the like.

5

6 **Overview**

7 Exemplary methods, systems, and devices are disclosed for probabilistic  
8 scheduling of tasks. In general, probabilistic scheduling may be applied to one or  
9 more tasks that require resources, a timeslot, and may that may have associated  
10 constraints. If two tasks require the same resources and timeslot, they conflict.  
11 Probabilistic scheduling involves minimizing a total schedule cost. The cost is a  
12 function of the excluded tasks. Cost is calculated from probability values  
13 associated with requested resources.

16

17 **An Exemplary System for Probabilistically Scheduling Tasks**

18 Fig. 1 illustrates an exemplary scheduling engine 100 implementing  
19 operations for probabilistic scheduling of tasks. The scheduling engine 100  
20 includes a main task log 102 that has a list of candidate task containers 104  
21 representing tasks to be scheduled into a schedule state 122. The scheduling  
22 engine 100 uses a cost generator 120 to analyze the main task log 102 to determine  
23 which of the task containers 104 should be moved to the schedule state 122.

1        The main task log 102 may contain the task containers 104 or have a list of  
2        references (e.g., pointers) to the task containers 104. A task container 104 is  
3        broken out to show components of an exemplary task container 106. The  
4        exemplary task container 106 includes one or more resource containers 108, a  
5        timeslot 110, one or more constraints 112, and an interface 114. As discussed  
6        further below, each resource container 108 includes one or more named resources  
7        116 and defines selection criteria related to the named resources. The resource  
8        containers 108 may include other resource container, called sub-containers. Sub-  
9        containers may include yet other resource containers.  
10

11        Each resource container 108 provides an interface 118 whereby functions  
12        can communicate with the resource container 108 to facilitate scheduling of the  
13        task 104. Each of the named resources 116 provides an interface (not shown)  
14        through which other containers can communicate with the named resource 116.  
15        More specifically, the named resource interface (not shown) and the resource  
16        container interface 118 include callable functions that enable a calling function to  
17        determine whether the named resource 116 or the resource container 108 influence  
18        (e.g., compete with, or support) a specified named resource or resource container.  
19        Exemplary types of resource containers are an ‘OR’ container, an ‘AND’ container,  
20        an ‘XOR’ container, and an ‘Integer-Set’ container, which are discussed in further  
21        detail below.  
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23  
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1        The timeslot 110 defines a timeslot in which the represented task is to  
2 occur. In one implementation, the timeslot 110 includes start time information,  
3 end time information, and duration information. The timeslot 110 may have an  
4 interface whereby modules can communicate with the timeslot 110 to facilitate  
5 scheduling of the represented task.

6        Each of the constraints 112 represents a time constraint between tasks  
7 represented by two of the task containers 104. In one implementation, each  
8 constraint 112 identifies another task container 104, and a time relationship  
9 between the task container 106 and the other task container 104. For example, a  
10 time relationship may indicate that the task represented by the task container 106  
11 must occur two hours before another task represented by another task container  
12 104. Constraints 112 are described in further detail below.

13       The scheduling engine 100 includes a cost generator 120 that communicates  
14 with the task containers 104 to generate costs associated with the tasks represented  
15 by the task containers 104. As used herein, the cost of a task is a numerical  
16 expression of the degree to which the task excludes or conflicts with another task.  
17 In one implementation, a total cost of a task is the sum of pair-wise costs  
18 associated with a pair of tasks. The costs can be calculated from probabilities that  
19 resources will or will not be allocated to a task. Calculating costs based on  
20 probabilities of resource allocation is discussed in further detail below.

1 A schedule state 122 provides the current state of the scheduled tasks. The  
2 schedule state 122 includes, or has a list of references to, the scheduled task  
3 containers 124 representing tasks that have been scheduled. During task  
4 scheduling, the schedule state 122 is used to determine whether candidate tasks  
5 104 in the main task log 102 can be added to the schedule state 122.  
6

7 In an implementation, the task containers 104, resource containers 108, and  
8 other modules shown in FIG. 1 are software objects or procedures that include data  
9 and methods that allow the scheduling engine 100 to schedule the task tasks  
10 associated with the task containers 104.

11 Fig. 2 is a hierarchical arrangement of an exemplary main task log having  
12 tasks with resource containers, and named resources. The exemplary main task log  
13 202 may be viewed as an inclusive “OR” container of a number of task containers  
14 204, 206, and 208, meaning that the scheduling engine will attempt to schedule as  
15 many of the task containers 204, 206, and 208 as possible. The task containers  
16 204, 206, and 208 are illustrated as nodes in the main task log 202. Below the task  
17 containers 204, 206, and 208 in the hierarchy are resource containers 210, 212, and  
18 214, respectively.  
19

20 The resource container 210 is an XOR container having named resource R1  
21 (216) and named resource R2 (218). Thus, the XOR container 210 chooses either  
22 named resource R1 (216) or named resource R2 (218). Named resources, such as  
23 the named resource R1 (216) and the named resource R2 (218), have associated  
24  
25

1 probabilities, q, that they will be selected. For example, the named resource R1  
2 (216) has a probability of ‘q1,’ and the named resource R2 (218) has probability  
3 ‘q2.’ The probabilities, q, dictate the likelihood that a task will be excluded, and  
4 are used to generate costs associated with tasks.

5 To illustrate how probability values, q, may be used in probabilistic  
6 scheduling, exemplary values for ‘q1’ and ‘q2’ are described. In an  
7 implementation, ‘q1’ and ‘q2’ are assigned default values of 50%, meaning that  
8 they are both equally likely to be selected in the XOR container 210. In this or  
9 another implementation, the default values for ‘q1’ and ‘q2’ may be user-adjusted  
10 to make one of the named resources R1 (216) or R2 (218) more likely selected  
11 than the other. Thus, in this implementation, the user can express a preference for  
12 one resource over another. The values, ‘q’, may be referred to as probabilities,  
13 weights, or preference values herein.

16 As tasks get scheduled and resources are allocated to scheduled tasks, the  
17 probability values, q, can change because of dependencies among tasks and  
18 resources. For example, the probability ‘q1’ may start out as 50%, but if named  
19 resource R1 (216) is selected, the value ‘q1’ can be changed to 1 (i.e., 100%).  
20 Another named resource R3 (220) (discussed further below) has a default  
21 probability value, q3, of 1, because the resource R3 (220) is the only named  
22 resource in its container, resource container 212; however, if the named resource  
23 R3 (220) is the same as the named resource R1 (216), and the two resources are  
24  
25

1 required simultaneously, the probability value  $q_3$  will be adjusted to 0 when the  
2 named resource R1 (216) is selected and scheduled. Thus, the probability values,  
3  $q$ , are a function of the current schedule state. Probability values and how they are  
4 dynamically adjusted are discussed in further detail below.

5 The resource container 212 is an XOR container with only one named  
6 resource R3 (220). Thus, the named resource R3 (220) is required for the task 206.  
7 In another implementation, singly required resources, such as named resource R3  
8 (220) need not be in an XOR container.

9 The resource container 214 is an AND container, meaning that the resource  
10 container chooses all of its components. As shown, the AND container 214  
11 includes and XOR container 222 and a named resource R4 (224). The XOR  
12 container 222 has three named resources, named resource R5 (226), named  
13 resource R6 (228), and named resource R7 (230). The XOR container 222 selects  
14 one of the resources 226, 228, or 230. The AND container 214 then chooses both  
15 the resource selected by the XOR container 222 and the named resource R4 (224).

16 Throughout the description, reference is made to ‘competition tables.’ A  
17 competition table relates tasks using cost values. In one implementation, a pair-  
18 wise cost is generated for each pair of tasks. The total cost for a task is the sum of  
19 the pair-wise costs associated with the task. The pair-wise costs are generated  
20 based on the probability values,  $q$ . An exemplary competition table can be  
21 illustrated with reference to the hierarchy shown in FIG. 2.

1 Using the hierarchy of Fig. 2 as an example, assume that named resource  
2 R1 (216), named resource R3 (220), and named resource R5 (226) are all equal to  
3 resource ‘a.’ Further assume that named resource R2 (218), and named resource  
4 R6 (228) are both equal to resource ‘b.’ Also assume that named resource R7  
5 (230) is equal to resource ‘c’ and that named resource R4 (224) is equal to  
6 resource ‘d.’ Assume also that no tasks have been scheduled. Thus, the schedule  
7 state is in the null state. Finally, assume that no preferences have been assigned to  
8 the probability values,  $q$ ; i.e., within an XOR container, the ‘ $q$ ’ values are equal.  
9 The foregoing assumptions may be expressed logically as follows:

10  
11 Task A:  $(a \mid b)$  (Task A requires ‘a’ xor ‘b’)  
12 Task B:  $a$  (Task B requires ‘a’)  
13 Task C:  $(a \mid b \mid c) \& d$  (Task C requires ‘a’ xor ‘b’ xor ‘c’ and ‘d’)

14 With the foregoing assumptions, the corresponding competition table is as  
15 shown in Table 1, referred to as the main competition table:  
16

17 **Table 1**

Main	Task A	Task B	Task C	Total Cost
Task A	0	1/2	1/3	5/6
Task B	1/2	0	1/3	5/6
Task C	1/3	1/3	0	2/3

21  
22 In Table 1, an intersection between column labeled with a task and a row  
23 labeled with a task is a pair-wise cost. In one implementation, the pair-wise cost  
24 between Task A and Task B is equal to the probability that Task A will exclude  
25

1 Task B. For example, the pair-wise cost of Task A and Task B is  $\frac{1}{2}$ . The column  
2 labeled 'Total Cost' provides the total costs associated with each of the Tasks, A,  
3 B, and C. As shown, the minimum cost task is Task C.

4 A cost generator in the scheduling engine can generate task costs, such as  
5 those shown in the competition table, Table 1. The cost generator may also  
6 tabulate the costs as shown. To develop a competition table the cost generator  
7 queries the task containers iteratively for pair-wise probabilities that they compete  
8 with each other task container. For example, the cost generator can query the task  
9 container A 204 for the probability that the task container A 204 competes with  
10 task container B 206 and the probability that the task container A 204 competes  
11 with the task container C 208. The cost generator uses a probabilistic interface to  
12 the task containers 204, 206, and 208 to query the task containers 204, 206, and  
13 208 in order to generate the pair-wise costs. Using the pair-wise costs, the cost  
14 generator can calculate the total costs associated with each task.

17 As discussed, resource and task containers provide a probabilistic interface  
18 to facilitate probabilistic scheduling. The following pseudocode function  
19 signatures comprise an exemplary probabilistic interface:  
20

```
Probability competes(S, A) :  
Probability supports(S, A)  
boolean onSelect(S, A)  
boolean onExclude(S, A)  
Probability prior(S)  
boolean mutually_exclusive(A)  
boolean overlap(A)  
boolean preCondition (S)  
boolean execute(S),  
boolean undo(S),
```

1                   wherein ‘S’ represents a schedule state and ‘A’ represents a container (e.g.,  
2                   task container, resource container) or a named resource.  
3

4                   A function call ‘B.competes(S, A)’ returns the probability that an input  
5                   container or resource ‘A’ excludes the called container, ‘B’, given the schedule  
6                   State ‘S’. For example, if ‘A’ and ‘B’ need simultaneous access to unique  
7                   resources ‘a’ or ‘b’ (exclusive ‘OR’, expressed as  $(a \mid b)$ ) then the function call  
8                   ‘B.competes(S, A)’ returns  $\frac{1}{2}$ , assuming independence and a random selection of  
9                   ‘a’ and ‘b’ for containers ‘A’ and ‘B’. The reason that the probability is  $\frac{1}{2}$  in the  
10                  previous example is because there is a  $\frac{1}{4}$  probability that ‘a’ will be randomly  
11                  selected for both ‘A’ and ‘B’ and a  $\frac{1}{4}$  probability that ‘b’ will be randomly selected  
12                  for both ‘A’ and ‘B’.  
13

14                  Continuing with the example, using containers ‘A,’ and ‘B,’ state ‘S,’ and  
15                  resource requirements  $(a \mid b)$ , the function call ‘B.competes(S, A)’ returns a value  
16                  different from  $\frac{1}{2}$  if the state ‘S’ already has one of the resources, ‘a’ and ‘b,’  
17                  allocated. For example, if the state already has resource ‘b’ allocated, then  
18                  resource ‘b’ is not available for selection and allocation to either container ‘A’ or  
19                  ‘B’; therefore, in this particular illustration, the function call ‘B.competes(S, A)’  
20                  returns 1, meaning that container ‘A’ will exclude container ‘B’ if ‘A’ is chosen.  
21

22                  With regard to function ‘supports(),’ a function call ‘B.supports(S, A)’  
23                  returns the probability that without container ‘B’, container ‘A’ will fail. For  
24

1 example, if container ‘A’ requires resources (a | b) (i.e., either resource ‘a’ or  
2 resource ‘b’, but not both), and container ‘B’ makes resource ‘a’ available, then the  
3 call ‘B.supports(S, A)’ returns probability  $\frac{1}{2}$ ; i.e., there is a  $\frac{1}{2}$  probability that  
4 without container ‘B,’ container ‘A’ will be excluded.

5 The scheduling engine uses the above functions to determine whether a  
6 container and a named resource compete or support each other. For example, the  
7 scheduling engine can call ‘B.competes(S, a)’ to determine if selection and  
8 allocation of named resource ‘a’ excludes container ‘B,’ given state S. As another  
9 example, the scheduling engine can call ‘B.supports(S, a)’ to determine if  
10 exclusion of container ‘B’ excludes named resource ‘a,’ given state S.

12 Turning to the onSelect() function, a function call ‘B.onSelect(S, A)’  
13 returns ‘false’ if the scheduling of ‘A’ excludes ‘B’ and returns ‘true’ otherwise.  
14 The function ‘B.onSelect(S, A)’ is typically called when container ‘A’ overlaps  
15 with ‘B,’ and ‘A’ has been selected and executed successfully by the scheduling  
16 engine. The term ‘overlapping’ means that a container has some bearing on, and  
17 may influence, the success or failure of another action. Thus, container ‘A’  
18 overlaps container ‘B’ because containers ‘A’ and ‘B’ have common members  
19 (e.g., resources), the selection of which may cause ‘A’ to exclude ‘B’ and vice  
20 versa. Overlap is discussed in further detail below.

23 Regarding the function ‘onExclude(),’ a function call B.onExclude(S, A)  
24 returns either ‘true’ or ‘false’ based on dependencies between container ‘B’ and  
25

1 container ‘A.’ The call `B.onExclude(S, A)` returns ‘false’ if container ‘B’ is  
2 excluded when overlapping action ‘A’ has been excluded or has failed to execute,  
3 and returns ‘true,’ otherwise.

4 The function ‘prior(S)’ returns a probability that a container will succeed  
5 (i.e., be scheduled) given State S. For example, if in the state S resources ‘a’ and  
6 ‘b’ were previously allocated and container ‘B’ requires  $(a \mid b \mid c)$  (i.e., one and  
7 only one of resources ‘a,’ ‘b,’ and ‘c’), the function call ‘`B.prior(S)`’ returns 1/3,  
8 assuming an independent random selection of resources ‘a,’ ‘b,’ and ‘c’.

9 The function ‘overlap(A)’ returns ‘true’ if the called container or resource  
10 overlaps with container ‘A.’ For example, if container ‘B’ requires resources ‘a’  
11 and ‘b’ (expressed as  $(a \& b)$ ) and ‘A’ requires resource ‘a’ simultaneously, then  
12 the call ‘`B.overlap(A)`’ returns ‘true.’

13 The function ‘preCondition(S)’ estimates whether the container can be  
14 successfully executed given State S. `B.preCondition(S)` returns false if B will  
15 certainly fail in schedule state S, and true otherwise.

16 The function call ‘`B.execute(S)`’ attempts to execute container ‘B’ in the  
17 schedule ‘S’ and returns ‘true’ if ‘B’ is successfully executed; if ‘B’ cannot  
18 successfully execute, the function call returns ‘false’. If the function `B.execute(S)`  
19 returns false, a function ‘`B.undo(S)`’ can be called to undo (i.e., reverse) side-  
20 effects that may have occurred during the failed attempt at execution. For  
21  
22  
23  
24  
25

1 example, the function B.undo(S) deallocates any resources that were allocated, or  
2 deschedules any tasks that were scheduled during the failed attempt at execution.

3 The function ‘mutually\_exclusive(a)’ is provided by named resources as  
4 well as containers. The function ‘mutually\_exclusive’ returns an indication as to  
5 whether two resources or containers are mutually exclusive. For example, in one  
6 implementation, the function call ‘b.mutually\_exclusive(a)’ returns ‘true’ if ‘a’  
7 excludes ‘b’. In another implementation, the function call  
8 ‘b.mutually\_exclusive(a)’ returns a probability that ‘a’ excludes ‘b.’  
9

10 With regard to the probabilistic interface, the actual implementation of the  
11 interface functions varies depending on the type of container. Below, exemplary  
12 implementations of the ‘competes()’ function are illustrated for the XOR  
13 container, the AND container, the OR container and the task container.

14 An XOR container, such as XOR containers 210, 212, and 222, is a  
15 resource container from which one, and no more than one resource is to be  
16 selected. Given a resource (i.e., a named resource or resource container), an XOR  
17 container determines the probability that the XOR container competes with the  
18 resource. The probability that an XOR container competes with a named resource  
19 ‘a’ is the sum over all the XOR container’s member resources, ‘c,’ having  
20 probabilities ‘ $q_c$ ’ as shown in the expression below:  
21  
22

$$23  
24 p(\text{XOR competes with } 'a') = \sum q_c \times c.\text{competes}(a),  
25$$

1  
2 The foregoing expression states that the probability that an XOR container  
3 competes with a single resource allocation, 'a', is equal to the sum of the  
4 probabilities,  $q_c$ , that the XOR container will use an option, 'c', times the  
5 probability that that option will exclude 'a'.

6 In one implementation, an XOR container maintains a competition sub-  
7 table that tabulates how each of its member resources competes with other tasks in  
8 the main task log. The competition sub-table is used to determine the cost of each  
9 selection and re-evaluate competition probabilities as resources are allocated to  
10 tasks and tasks are scheduled. Referring again to the above example, from which  
11 Table 1 was generated, an exemplary competition sub-table can be generated for  
12 the XOR containers 210, 212, and 214 (Tables 2, 3, and 4, respectively):

13 **Table 2**

Task A	Task B	Task C	Total Cost
a	1	1/3	4/3
b	0	1/3	1/3

16 **Table 3**

Task B	Task A	Task C	Total Cost
a	1/2	1/3	5/6

20 **Table 4**

Task C	Task A	Task B	Total Cost
a	1/2	1	3/2
b	1/2	0	1/2
c	0	0	0

1 In an implementation, XOR containers exclude any member resources  
2 whose pre-condition fails (i.e., any resource that cannot be selected because of the  
3 schedule state). In this implementation, when a pre-condition fails for such a  
4 resource, the associated XOR container assigns probability value of zero to the  
5 member resource whose pre-condition fails. If the user has not applied any  
6 preferences to the remaining member resources and the schedule state is the null  
7 state, equal probability values are applied to the XOR container's remaining  
8 member resources. Thereafter, selection probabilities are assigned on the basis of  
9 minimum cost, as discussed herein.

10 With regard to the pre-condition() function of an XOR container, in one  
11 implementation the XOR container pre-condition() function returns 'true' if any of  
12 the XOR container's member's pre-condition() functions return 'true.'

13 With regard to the execute() function of an XOR container, in one  
14 implementation, successful execution of any members of the XOR container  
15 results in returning 'true.' In response to receiving a call to 'execute()', an XOR  
16 container calls the execute() functions of the XOR container's members in order of  
17 least cost. If a call to an execute() function returns 'false' any side-effects (e.g.,  
18 resource allocations, scheduled tasks, etc.) of the execution are reversed by calling  
19 the 'undo()' function prior to calling the execute() function of the next container  
20 member. When one of the member's execute() function returns 'true,' the XOR  
21 container selects that member.

22 An AND container, such as the AND container 214, is a resource container  
23 for which all member resources or member containers are required for a task. For  
24 example, the AND container 214 requires both the XOR container 222 and the  
25

1 named resource R4 (224) in order for the task container 208 to be successfully  
2 scheduled.

3 Turning to the probabilistic interface for an AND container, the competes()  
4 function for an AND container returns the probability that an AND container  
5 excludes another container. The probability that container ‘A’ excludes an AND  
6 container is equal to one minus the probability that all members ‘ $c_i$ ’ of the AND  
7 container do not compete with ‘A’ (independence assumption). That is:

$$8 \\ 9 1 - (1 - c_1.competes(A)) \times (1 - c_2.competes(A)) \times \dots \times (1 - c_i.competes(A)).$$

10  
11 The ‘pre-condition()’ function of an AND container returns true only if all  
12 the AND containers’ member resources’ pre-condition() functions return true. The  
13 ‘execute()’ function in an AND container returns ‘true’ only if all members of the  
14 AND container execute successfully. AND containers contribute their own  
15 member resources to the competition table of any member containers because  
16 resource dependencies may exist between member containers of AND containers.

17 Turning now to an OR container, an OR container is a container that  
18 designates a selection of member resources such that at least 1 member is selected  
19 and the weight of selected members is maximized, given the current schedule state.  
20 If at least 1 member cannot be selected because all members are excluded by other  
21 tasks, the OR container will not be successfully scheduled. With regard to the  
22 competes() function as it pertains to an OR container, the probability that an OR  
23 container excludes another action, ‘a’, is the sum over all OR container members,  
24 ‘c’, of the viability of a member resource, ‘c’, times the probability that ‘c’

1 excludes 'a'. The competes() function for an OR container may be implemented  
2 as a simple iterative calculation.

3 Viability of a task represents the likelihood that the task will survive to the  
4 final schedule. The viability of a task depends on the availability of containers or  
5 resources. In turn, the viability of a task can influence the viability of other tasks  
6 that may use the same resources and containers. In one implementation of the  
7 scheduler, if a task 'A' uses a particular resource in a particular timeslot and has a  
8 high viability, another task 'B' that must use the same resource in the same time  
9 slot will have a low viability. For example, a task that excludes one other equally  
10 weighted task has a 50/50 viability. A task that requires an already allocated  
11 resource has 0 viability. A task of zero cost has viability 1.

12 In response to a call to the 'execute()' function in an OR container, the OR  
13 container iteratively calls the execute() function of the OR container's members.  
14 In one implementation, the OR container maintains a competition sub-table that  
15 relates each member resource to the other tasks with a numerical cost value, as  
16 illustrated above. The OR container selects randomly between members of  
17 minimum cost and executes (or if necessary, excludes) each member until all  
18 members are processed.

19 A task container, such as the task container 204, the task container 206, and  
20 the task container 208, uses combinations of named resources, resource containers,  
21 timeslots, and constraints to represent a task. Named resources and resource  
22 containers are discussed above in detail. A timeslot, such as the timeslot 110 in  
23 Fig. 1, represents a time allocation of the associated task as a set of start-time  
24 choices with associated probabilities. A timeslot can be defined using notation [x-  
25

1 y-z], wherein ‘x’ represents the earliest possible time to start, ‘y’ represents the  
2 required duration, and ‘z’ represents the latest possible time to finish.

3 A timeslot can be implemented as an XOR container, wherein possible  
4 times for the timeslot are named resources discussed above. For example, if a task  
5 is defined as [1-2-5] (i.e., the timeslot requires two hours sometime between the  
6 hours of 1:00 and 5:00), the time periods 1:00-3:00, 2:00-4:00, and 3:00-5:00 can  
7 be grouped into an XOR container as named resources.

8 A first timeslot competes with a second time slot if any portion of a selected  
9 time period for the first timeslot overlaps with a portion of a selected time period  
10 for the second timeslot. The compete() function for a timeslot returns a probability  
11 much like an XOR container discussed above. For example, if a first timeslot is  
12 defined as [0-4-8], and a second timeslot is defined as [0-4-8], the probability that  
13 the first timeslot competes with the second time slot is 23/25.

14 A constraint, such as the constraints 112 in Fig. 1, represents any time-  
15 constraint between two tasks. A constraint may be implemented as an instance of  
16 a timeslot. In one implementation, one constraint excludes another constraint if  
17 the constraints have the same constraint-ID and according to the probability that  
18 one or both of the constraints will not be satisfied. Thus, for example, if two  
19 constraints have same constraint-ID, they might conflict, depending on what sort it  
20 is; otherwise, the two constraints will not conflict.

21 In one implementation, a constraint excludes the constraint’s associated  
22 timeslot if constraint’s time and the timeslot’s time are not the same. To illustrate,  
23 assume Task A must follow Task B by more than two hours. Such a two hour time  
24 constraint can be implemented by two “constraint” actions added to both tasks  
25 which include a set of timeslots. These constraints exclude each other according to

1 the probability that they will use conflicting timeslots, i.e., not within two hours.  
2 Also, the constraints will exclude their associated task's timeslot, according to the  
3 probability that the constraint needs a timeslot that the task can't have.

4 In one implementation, for a task to be viable, the task's required resources  
5 must be available, the task's timeslot must be available, and the task's constraints  
6 must be satisfied. The following expressions can be used to determine the viability  
7 of a task:

8

9 (1)  $R = f(r_n)$ , and  
10 (2)  $V_{Task} = (c_1 \& c_2 \& c_3 \& \dots \& c_i) \& (T | R)$ ,

11 where  $f(r_n)$  represents a function of 'n' resources (e.g., XOR, AND, OR, or any  
12 combination thereof), R represents the viability of the resources ' $r_n$ ', ' $c_i$ ' is a  
13 Boolean indicator of whether the  $i^{\text{th}}$  constraint is satisfied, and T is a Boolean  
14 indicator of whether an exclusive timeslot can be obtained.

15 Thus, equation (2) above indicates that the viability,  $V_{Task}$ , of a first Task is  
16 non-zero if all the constraints of the first Task are satisfied and either an exclusive  
17 timeslot, T, can be obtained, or an exclusive resource allocation, R, can be  
18 obtained. With regard to cost calculation as it relates to timeslot, T, and resource  
19 allocation, R, the probability that another task's timeslot excludes its own timeslot  
20 is multiplied by the probability that the task's resources exclude the task's  
21 resources, and vice versa.

22

23

24

1      Turning to the interface for a task container, the overlap() function,  
2      competes() function, precondition() function, and execute() function are described  
3      as follows in terms of the task container.

4      For task container B, the function call B.overlap(A) returns false if either  
5      the timeslot or resource requirements of container B do not overlap with the  
6      timeslot or resource requirements of container A.

7      For task container B, the function call B.competes(A) returns the  
8      probability that a constraint between A and B excludes the task container B plus  
9      the probability that B is not excluded by a constraint and a timeslot excludes B and  
10     a resource allocation excludes B. Thus, the function B.competes(A) can be  
11     expressed as follows:

12      $c.competes(A) + ((1-c.competes(A)) \times (T.competes(A) \times R.competes(A))),$   
13     where 'c' represents a constraint container of B, T represents a timeslot container  
14     of B, and R represents a resource container of B.

15     For task container B, the function call B.precondition(S) returns true if at  
16     least one time period is available in schedule state S, which satisfies the timeslot  
17     container in B, and has the available resources that are required by task B. The  
18     function call B.precondition(S) may be viewed as the intersection of resource-free  
19     times in state S that satisfy both the B container's timeslot and resource  
20     requirements.

1       With regard to the execute(S) function for a task container, one  
2 implementation of the execute(S) function attempts to identify a time slot and  
3 resource allocation that intersect with available corresponding time slots and  
4 resources in state S. In this implementation, the execute(S) function randomly  
5 selects a minimum cost time slot. Resources required by the task container, but  
6 that are unavailable at the selected time slot, are assigned a viability of zero. For  
7 those resources that are available in the selected time slot, resources are selected  
8 according to minimum cost. If no consistent allocation is found, the selected time  
9 slot is assigned a viability of zero, and another time slot is randomly selected.  
10

11       An alternative implementation of the execute(S) function for a task  
12 container involves the use of prior probabilities. In this implementation, prior  
13 viabilities of time slots associated with the task are iteratively multiplied by the  
14 probability that required resources are available during each time slot. A ratio is  
15 generated of resource viabilities of available resources to total possible resources.  
16 Resource viability is then recomputed according to the viability of the task's  
17 available timeslots; that is, ratio of viability of timeslots the task can use to total  
18 available timeslots.  
19

21

### Exemplary Operations for Probabilistically Scheduling Tasks

23       Fig. 3 is a scheduling operation flow 300 having exemplary operations by  
24 which a scheduling engine (e.g., the scheduling engine 100, Fig. 1) may  
25

1 probabilistically schedule tasks. Upon entering the operation flow 300, a current  
2 scheduled state (e.g., the schedule state 122, Fig. 1) may have tasks currently  
3 scheduled. It is assumed that the current scheduled state is passed into the  
4 scheduling operation flow 300 or is otherwise available. In a populating operation  
5 302, the main task log of the scheduling engine is populated with the tasks and  
6 their associated resource requirements, timeslots, constraints, and preference  
7 weights. The tasks in the main task log may be referred to as candidate tasks,  
8 which are being considered for scheduling.

9  
10 A generating operation 304 generates costs associated with each of the  
11 candidate tasks. As discussed above, a cost of a candidate task represents  
12 numerically the degree to which the candidate task conflicts with and causes the  
13 exclusion of other candidate tasks. The costs generated in the generating operation  
14 304 are a function of probabilities of selecting resources for each of the candidate  
15 tasks. An exemplary generating operation 304 is illustrated in Fig. 4 and is  
16 discussed in further detail below. The output of the generating operation 304 is a  
17 list of candidate tasks in order of least cost to highest cost.

18  
19 A query operation 306 determines whether tasks in the main task log are  
20 viable with respect to the schedule state. Viability can be determined by calling the  
21 precondition() function of each task container in the main task log. The viability  
22 of a task is zero if the precondition() function returns false (i.e., zero probability of  
23 being scheduled). The viability is set to zero if call to the precondition() functions  
24  
25

1 fail. If at least one call to the precondition() functions returns true then the query  
2 operation 306 branches ‘YES’ to an executing operation 308.

3 An executing operation 308 executes the least cost candidate task using the  
4 schedule state. The executing operation 308 calls the execute() operation of the  
5 least cost candidate task, which attempts to insert the least cost candidate task in  
6 the current schedule without any conflicts with previously scheduled tasks. One  
7 implementation of the executing operation 308 iterates through each of the  
8 scheduled tasks in the current schedule, and determines for each scheduled task  
9 whether the least cost candidate task requires the same resources in the same  
10 timeslot as the scheduled task, using the competes() functions of the task’s member  
11 containers. If the least cost candidate task conflicts with one of the scheduled  
12 tasks, the executing operation is not successful. If the least cost candidate task  
13 does not conflict with any of the scheduled tasks, the executing operation is  
14 successful.

15 A query operation 310 determines whether the executing operation 310 was  
16 successful. If the executing operation 310 was not successful, the operation flow  
17 300 branches “NO” back to the executing operation 310. Upon returning to the  
18 executing operation, the next least cost candidate task is executed with respect to  
19 the current schedule state as discussed above.

20 If it is determined in the query operation 310 that the executing operation  
21 308 was successful, the operation flow branches ‘YES’ to a scheduling operation  
22

1       312. The scheduling operation 312 schedules the successfully executed task into  
2       the current schedule and updates the current schedule state. In one implementation  
3       of the scheduling operation 312, the task container representing the scheduled task  
4       is moved into the current schedule state 122, Fig. 1. The scheduling operation 312  
5       disables options that are not selected as a result of the scheduled task.

6       An adjusting operation 314 adjusts the resource probabilities (i.e., the ‘q’  
7       values, discussed above) based on the scheduled task. An implementation of the  
8       adjusting operation 314 sets ‘q’ to zero for those resource containers that are no  
9       longer viable because of the scheduled task. The adjusting operation 314 may also  
10      set the ‘q’ value to 1 for those named resources and resource containers that were  
11      allocated to the scheduled task.

12      The generating operation 304 re-generates the costs of the task containers  
13      and resource containers based on the adjusted probabilities. As discussed above,  
14      the generating operation creates a main competition table that includes pair-wise  
15      costs relating every pair of tasks in the main task log and total costs. The  
16      generating operation 304 may generate other competition tables associated with  
17      resource containers that include costs for resource selections for each resource  
18      container. Re-generating the costs is the same procedure as discussed above, but  
19      the probabilities may be different on subsequent iterations. The query operation  
20      306 again determines whether any viable tasks (i.e., any tasks whose probability of  
21  
22  
23  
24  
25

1 survival is non-zero) remain in the competition tables. If no viable tasks remain,  
2 the scheduling operation branches ‘NO’ to a return operation 316.

3 Fig. 4 is a cost generating operation flow 400 having exemplary operations  
4 for generating costs associated with tasks. A receiving operation 402 receives a  
5 task ‘B’ for pair-wise cost analysis with all other candidate tasks. A selecting  
6 operation 404 selects another task ‘C’ to create a pair of tasks for cost analysis. A  
7 requesting operation 406 requests probabilities that ‘B’ competes from each  
8 container in ‘C.’

9 In the requesting operation 406, the compete(B) function is called for each  
10 container in ‘C’, as well as each sub-container, each sub-sub-container, and so on.  
11 For example, with reference to the exemplary hierarchy of Fig. 2, the requesting  
12 operation 406 calls compete(B) of the AND container 214, which calls the  
13 compete(B) function of the XOR container 222 and the compete(B) function of the  
14 named resource R4 (224). The results of the requesting operation are one or more  
15 probabilities that ‘B’ competes with containers in ‘C’.

16 A calculating operation 408 calculates the pair-wise cost based on the  
17 probabilities obtained in the requesting operation 406. In one implementation, the  
18 pair-wise probability is the sum of all probabilities that ‘B’ will compete with each  
19 of the containers in ‘C.’ In another implementation of the calculating operation  
20 408, the pair-wise cost is a function of the probability that ‘B’ competes with ‘C’.

1       A query operation 410 determines whether any more tasks remain for pair-  
2       wise cost analysis with respect to task ‘B’. If more tasks remain, the generating  
3       operation 400 branches ‘YES’ to the selecting operation 404, wherein the next task  
4       is selected for cost-analysis. If no more tasks remain, the generating operation 400  
5       branches ‘NO’ to a repeating operation 412, wherein the generating operation 400  
6       is repeated for a next task in the main log. After all pair-wise and total costs have  
7       been generated and tabulated by the generating operation 400, the generating  
8       operation 400 ends at a returning operation 414.

10

11 **Exemplary Scenario**

12       An example is provided below to illustrate how probabilistic scheduling  
13       may be employed with resource containers and using the ‘minimum cost’ criterion.  
14  
15       Assume four tasks (A, B, C and D) each require some combination of resources a,  
16       b, and c as follows:

17  
18       A:    (a | c)        -- A requires a or c (XOR)  
19  
20       B:    (b | c)        -- B requires b or c (XOR)  
21  
22       C:    (c)            -- C requires c (XOR)  
23  
24       D:    (a & b)       -- D requires a and b (AND)

25  
26       Tasks A, B, C, and D are all part of the main task log. From a null schedule  
27       state (i.e., no tasks scheduled), each task is initially assumed equally ‘viable’ (prob.  
28       of survival equal 1) and each option (e.g., a or b) is assigned equal probability.

1 Competition tables are generated with pair-wise costs,  $X_{ij}$  (probability that i  
2 excludes j), as shown in Table 5:

Main	A	B	C	D	Total Cost	Viability
A	0	1/4	1/2	1/2	5/4	4/9
B	1/4	0	1/2	1/2	5/4	4/9
C	1/2	1/2	0	0	1	1/2
D	1/2	1/2	0	0	1	1/2

11 That is to say, the probability  $X_{AB}$  that A excludes B is  $1/2$  (A chooses c)  $\times 1/2$   
12 (B chooses c) =  $1/4$ , and so on. Viability is calculated as  $1/(1+\text{TotalCost})$ .

13 Competition sub-table for each of the XOR container actions, A and B, are  
14 generated as shown in Tables 6 and 7 below:

A	B	C	D	Total Cost	Viability
a	0	0	1	1	1/2
c	1/2	1	0	3/2	2/5

B	A	C	D	Total Cost	Viability
b	0	0	1	1	1/2
c	1/2	1	0	3/2	2/5

1  
2 where the ‘Total Cost’ column (expected weight of viable resources excluded) is  
3 computed by adding up each exclusion probability times the probability that this  
4 resource is viable. This probability is initially set equal to the resource’s prior  
5 probability minus 1 for the null state.

6 The ‘viability’ column is computed for Table 5 (each probability that a task  
7 survives potential competitors). Entries in the MAIN table (Table 5) are then used  
8 to re-compute costs for each of the sub-tables (Table 6 and Table 7). The XOR  
9 sub-tables re-adjust their internal probabilities to select between tasks of minimum  
10 cost, which changes the  $X_{nk}$ . Viabilities are re-computed, and so on, until no  
11 further changes are made. Scheduling tasks from the MAIN table (Table 5)  
12 involves selecting arbitrarily between its minimum cost tasks, testing the pre-  
13 condition of the selected task and executing the task.

14 In this example, C and D start off as the most viable tasks. A and B select  
15 resources a and b respectively as their minimum cost options, and after 2 steps, the  
16 iteration ends with the resource selections shown below in Tables 8, 9, and 10:  
17

18 **Table 8**

A	B	C	D
a	0	0	1
c	0	1	0

23 **Table 9**

B	A	C	D
b	0	0	1

<b>c</b>	0	1	0
----------	---	---	---

**Table 10**

Main	A	B	C	D
A	0	0	0	1
B	0	0	0	1
C	0	0	0	0
D	1	1	0	0

## **Exemplary User Interfaces to Facilitate Probabilistic Scheduling of Tasks**

Fig. 5 illustrates a user interface 500 that may be employed by a scheduling engine (e.g., scheduling engine 100, Fig. 1) to receive scheduling input and present scheduling output. The exemplary user interface 500 is designed for an orthopedic surgery setting, in which nurses, consultants, anaesthetists, and operating room theatres are resources to be allocated to a number of patients requiring operations.

A task ID column 502 is a list of patients who require various operations. Check boxes 504 indicate which of the tasks in the column 502 have been scheduled, and which have not. In an early start column 506 a user can enter the earliest possible start time for an associated task. Thus, the MrK-HipReplacement cannot start before time '0'. A late finish column 508 provides the latest possible finish time for an associated task. A duration column 510 provides the duration of the task. The early start times, late finish times, and duration, collectively define a timeslot that can be used to probabilistically schedule the tasks in the task ID column 502 using methods discussed above.

1 A resource 1 column 512 lists consultant requirements for associated tasks.  
2 The MrI-HipReplacement can use either consultant1 or consultant2 (i.e., XOR). A  
3 resource 2 column 514 lists nurse requirements for associated tasks. The MrI-  
4 HipReplacement can use nurse1, nurse2, nurse3, or nurse4 (i.e., XOR). A resource  
5 column 516 lists anaesthetist requirements for associated tasks. The MrI-  
6 HipReplacement can use anaesthetist1, or anaesthetist2 (i.e., XOR). A resource4  
7 column 518 lists theatre requirements for associated tasks. The MrI-  
8 HipReplacement can use theatre1, or theatre2 (i.e., XOR). After a user has entered  
9 in the resource requirements and timeslot specifications, the user can select a  
10 submit button 520 to cause a scheduling engine to schedule the tasks.

11 Fig. 6 illustrates another user interface 600 that may be employed by a  
12 scheduling engine to receive scheduling input including constraints. Like the user  
13 interface of Fig. 5, the user interface 600 includes a list of tasks, early start time,  
14 late finish time, and duration, and resources. The user interface 600 also provides  
15 a constraints entry area 602, into which a user can enter constraints. As shown, the  
16 constraints are specified in terms of a temporal relationship between two tasks.  
17 Thus, as shown, the Consultant2-WardRound is to end 0 to 4 time units before the  
18 Ward Meeting starts. Constraints from the constraints entry area 602 can be  
19 incorporated into constraint containers as discussed above for probabilistically  
20 scheduling tasks.

21

## 22 An Exemplary Operating Environment

23 FIG. 7 illustrates one operating environment 710 in which the various  
24 systems, methods, and data structures described herein may be implemented. The  
25 exemplary operating environment 710 of FIG. 7 includes a general purpose

1 computing device in the form of a computer 720, including a processing unit 721,  
2 a system memory 722, and a system bus 723 that operatively couples various  
3 system components include the system memory to the processing unit 721. There  
4 may be only one or there may be more than one processing unit 721, such that the  
5 processor of computer 720 comprises a single central-processing unit (CPU), or a  
6 plurality of processing units, commonly referred to as a parallel processing  
7 environment. The computer 720 may be a conventional computer, a distributed  
8 computer, or any other type of computer.

9 The system bus 723 may be any of several types of bus structures including  
10 a memory bus or memory controller, a peripheral bus, and a local bus using any of  
11 a variety of bus architectures. The system memory may also be referred to as  
12 simply the memory, and includes read only memory (ROM) 724 and random  
13 access memory (RAM) 725. A basic input/output system (BIOS) 726, containing  
14 the basic routines that help to transfer information between elements within the  
15 computer 720, such as during start-up, is stored in ROM 724. The computer 720  
16 further includes a hard disk drive 727 for reading from and writing to a hard disk,  
17 not shown, a magnetic disk drive 728 for reading from or writing to a removable  
18 magnetic disk 729, and an optical disk drive 730 for reading from or writing to a  
19 removable optical disk 731 such as a CD ROM or other optical media.

20 The hard disk drive 727, magnetic disk drive 728, and optical disk drive  
21 730 are connected to the system bus 723 by a hard disk drive interface 732, a  
22 magnetic disk drive interface 733, and an optical disk drive interface 734,  
23 respectively. The drives and their associated computer-readable media provide  
24 nonvolatile storage of computer-readable instructions, data structures, program  
25 modules and other data for the computer 720. It should be appreciated by those

1 skilled in the art that any type of computer-readable media which can store data  
2 that is accessible by a computer, such as magnetic cassettes, flash memory cards,  
3 digital video disks, Bernoulli cartridges, random access memories (RAMs), read  
4 only memories (ROMs), and the like, may be used in the exemplary operating  
5 environment.

6 A number of program modules may be stored on the hard disk, magnetic  
7 disk 729, optical disk 731, ROM 724, or RAM 725, including an operating system  
8 735, one or more application programs 736, other program modules 737, and  
9 program data 738. At least one of the application programs 736 is a scheduling  
10 application operable to control scheduling of events or tasks that have resource  
11 requirements.

12 A user may enter commands and information into the personal computer  
13 720 through input devices such as a keyboard 740 and pointing device 742. Other  
14 input devices (not shown) may include a microphone, joystick, game pad, satellite  
15 dish, scanner, or the like. These and other input devices are often connected to the  
16 processing unit 721 through a serial port interface 746 that is coupled to the system  
17 bus, but may be connected by other interfaces, such as a parallel port, game port,  
18 or a universal serial bus (USB). A monitor 747 or other type of display device is  
19 also connected to the system bus 723 via an interface, such as a video adapter 748.  
20 In addition to the monitor, computers typically include other peripheral output  
21 devices (not shown), such as speakers and printers.

22 The computer 720 may operate in a networked environment using logical  
23 connections to one or more remote computers, such as remote computer 749.  
24 These logical connections may be achieved by a communication device coupled to  
25 or a part of the computer 720, or in other manners. The remote computer 749 may

1 be another computer, a server, a router, a network PC, a client, a peer device or  
2 other common network node, and typically includes many or all of the elements  
3 described above relative to the computer 720, although only a memory storage  
4 device 750 has been illustrated in FIG. 7. The logical connections depicted in FIG.  
5 7 include a local-area network (LAN) 751 and a wide-area network (WAN) 752.  
6 The LAN 751 and/or the WAN 752 can be wired networks, wireless networks, or  
7 any combination of wired or wireless networks. Such networking environments  
8 are commonplace in office networks, enterprise-wide computer networks, intranets  
9 and the Internal, which are all types of networks.

10 When used in a LAN-networking environment, the computer 720 is  
11 connected to the local network 751 through a network interface or adapter 753,  
12 which is one type of communications device. When used in a WAN-networking  
13 environment, the computer 720 typically includes a modem 754, a type of  
14 communications device, or any other type of communications device for  
15 establishing communications over the wide area network 752. The modem 754,  
16 which may be internal or external, is connected to the system bus 723 via the serial  
17 port interface 746. In a networked environment, program modules depicted relative  
18 to the personal computer 720, or portions thereof, may be stored in the remote  
19 memory storage device. It is appreciated that the network connections shown are  
20 exemplary and other means of and communications devices for establishing a  
21 communications link between the computers may be used.

22 Although some exemplary methods, devices and exemplary systems have  
23 been illustrated in the accompanying Drawings and described in the foregoing  
24 Detailed Description, it will be understood that the methods and systems are not  
25 limited to the exemplary embodiments disclosed, but are capable of numerous

1 rearrangements, modifications and substitutions without departing from the spirit  
2 set forth and defined by the following claims.

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